Exercises 0: 11, 14, 16, 17, 19, 20ai

## Additional exercises:

1. Let  $\phi \colon A \to B$  and  $\chi \colon B \to C$  be two maps. Show that:

(a) If  $\chi \circ \phi$  is surjective, then  $\chi$  must be surjective.

(b) If  $\chi \circ \phi$  is injective, then  $\phi$  must be injective.

2. Determine whether the following maps are invertible.

(a)  $\phi : \mathbb{R} \to \mathbb{R}$ , where  $\phi(x) = \frac{5+3x}{2}$ 

(b)  $\phi : \mathbb{R} \to \mathbb{R}$ , where  $\phi(x) = x^2 - 4$ .

3. Let  $\phi:A\to B$  and  $\chi:B\to C$  be maps. Prove that if  $\phi$  and  $\chi$  are both surjective, then  $\chi\circ\phi$  is surjective.