

1. Find $\oint_C -y dx + 2x dy$ where C is the part of the circle $x^2 + y^2 = 1$ from $(1, 0)$ to $(0, 1)$.

2. Find $\oint_C -xy dx + x^2 dy$ where C is the triangle bounded by $(1, 0)$, $(3, 0)$, and $(2, 3)$, oriented counterclockwise.

3. Integrate $f(x, y) = xy^2$ along the circle $x^2 + y^2 = 4$ from $(2, 0)$ to $(0, 2)$.

4. Find the counterclockwise circulation of $\vec{F} = \langle 3x, 2y \rangle$ around the boundary of the region $0 \leq x \leq \pi$, $0 \leq y \leq \sin x$.

5. Let $\vec{F}(x, y) = \langle -x^2y, xy^2 \rangle$, let C be the circle $x^2 + y^2 = a^2$, oriented counterclockwise, and let R be the region in the xy -plane bounded by C . Verify Green's Theorem by evaluating both sides of the equation in the theorem and checking that they are equal.

6. Let $\vec{F}(x, y) = \langle x^2 + 4y, x + y^2 \rangle$ and let C be the square bounded by $x = 0$, $x = 1$, $y = 0$, $y = 1$. Use Green's Theorem to find the counterclockwise circulation for this \vec{F} and C .

7. Apply Green's Theorem to evaluate

$$\oint_C 3y dx + 2x dy$$

where C is the boundary of the region $0 \leq x \leq \pi$, $0 \leq y \leq \sin x$.

8. Evaluate $\int_C (x + y^2)/\sqrt{1 + x^2} ds$ where C is the part of the curve $y = x^2/2$ from the point $(0, 0)$ to the point $(1, 1/2)$.

9. Find the work done by $\vec{F} = \langle z, x, y \rangle$ over the helix $\vec{r}(t) = \langle \sin t, \cos t, t \rangle$ with $0 \leq t \leq 2\pi$.

10. Find the circulation of the field $\vec{F} = \langle -y, x \rangle$ over the ellipse $\vec{r}(t) = \langle \cos t, 4 \sin t \rangle$ with $0 \leq t \leq 2\pi$.

11. Evaluate $\int_C \sqrt{x^2 + y^2} ds$ along the curve $\vec{r}(t) = \langle 4 \cos t, 4 \sin t, 3t \rangle$ where $-2\pi \leq t \leq 2\pi$.
