

The following exercises are from the corresponding sections of the UC Berkeley custom edition of Lay, Nagle, Saff, & Snider, Linear Algebra and Differential Equations. Note that the section numbers and problem numbers ARE NOT the same as in Lay, Linear Algebra.

Exercises 2.1: 9, 11, 15, 16, 17, 20, 21, 27, 34

Exercises 2.2: 21, 25, 33, 34

Exercises 2.3: 7, 18, 19, 27, 36, 38

Exercises 3.1: 11, 13, 41

Additional Problems:

1. Let A and B be $n \times n$ matrices. Find a formula for $(A + B)^2$ in terms of $A^2, B^2, AB,$ and BA .
2. Let $I_2 = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ and $J_2 = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$. Show that the sum and product of two matrices $aI_2 + bJ_2$ and $cI_2 + dJ_2$ again has the same form, and that the formulas for the sum and product match those for complex numbers $a + bi$ and $c + di$.
3. Let $A = \begin{pmatrix} 2 & 0 & 2 \\ 0 & 1 & -1 \\ 1 & 1 & -1 \end{pmatrix}$. Solve the matrix equation $AX = B$ for a 3×2 matrix X . Hint: think about the expansion by columns of the matrix product AX .
4. Prove the Invertible Matrix Theorem. You may refer to any theorems we have done earlier in the class. (The solution to this is in the book, but it is a good exercise to try to do this on your own, without looking it up!)