

1. Consider the following parametric curves:

$$\mathbf{x}_1(t) = \begin{pmatrix} \cos t \\ \sin t \end{pmatrix}, \quad \mathbf{x}_2(t) = \begin{pmatrix} e^t \cos t \\ e^t \sin t \end{pmatrix}, \quad \mathbf{x}_3(t) = \begin{pmatrix} t \cos t \\ t \sin t \end{pmatrix}, \quad \mathbf{x}_4(t) = \begin{pmatrix} t - \sin t \\ 1 - \cos t \end{pmatrix},$$

$$\mathbf{x}_5(t) = \begin{pmatrix} t \\ t \end{pmatrix}, \quad \mathbf{x}_6(t) = \begin{pmatrix} t \\ t^2 \end{pmatrix}, \quad \mathbf{x}_7(t) = \begin{pmatrix} t^2 \\ t^2 \end{pmatrix}, \quad \mathbf{x}_8(t) = \begin{pmatrix} t^2 \\ t \end{pmatrix},$$

$$\mathbf{x}_9(t) = \begin{pmatrix} \cos t \\ \sin t \\ t \end{pmatrix}, \quad \mathbf{x}_{10}(t) = \begin{pmatrix} e^t \cos t \\ e^t \sin t \\ e^t \end{pmatrix}, \quad \mathbf{x}_{11}(t) = \begin{pmatrix} t \cos t \\ t \sin t \\ t \end{pmatrix}, \quad \mathbf{x}_{12}(t) = \begin{pmatrix} \cos t \\ \sin t \\ \cos^2 t \end{pmatrix}.$$

On the next page, pictures for these are given. For each one, match the parametrization with the picture.

2. For each of the following curves, find the velocity vector, the speed, the unit tangent vector, the linear acceleration, and the angular acceleration.

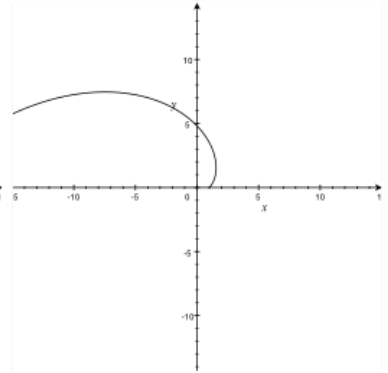
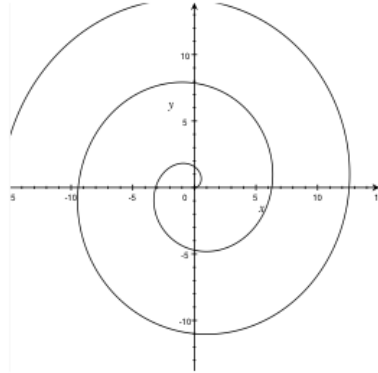
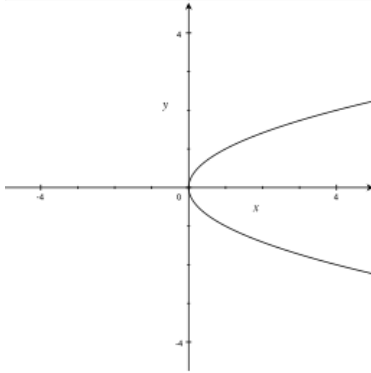
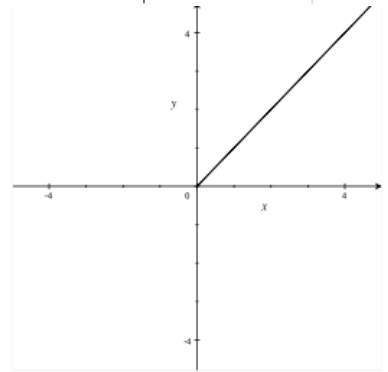
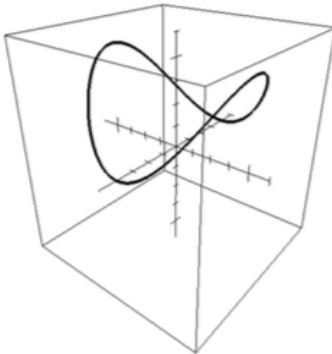
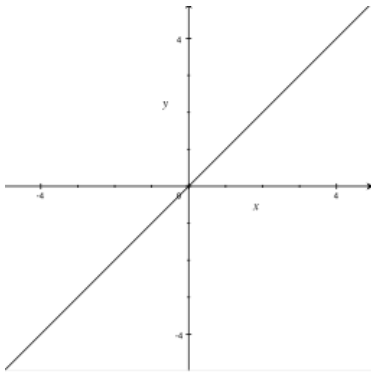
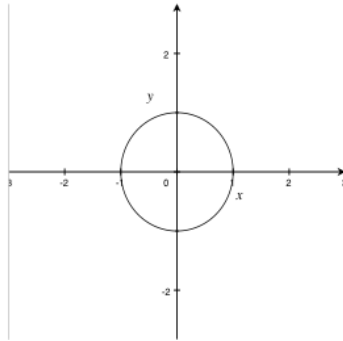
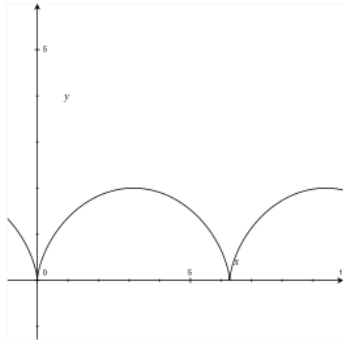
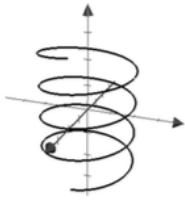
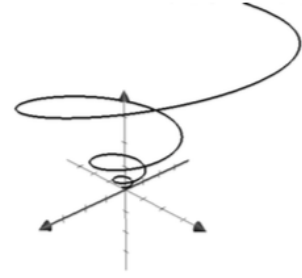
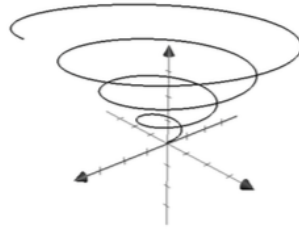
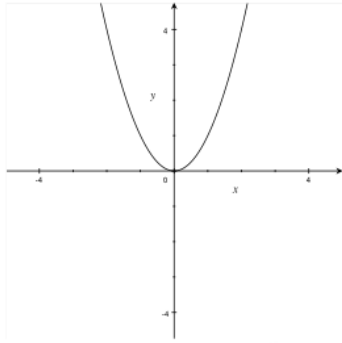
$$\mathbf{r}_1(t) = \begin{pmatrix} 3 + 2t \\ -1 - t \\ 5 - 2t \end{pmatrix}, \quad \mathbf{r}_2(t) = \begin{pmatrix} 3 \cos t \\ 3 \sin t \\ 4t \end{pmatrix}, \quad \mathbf{r}_3(t) = \begin{pmatrix} e^t \cos t \\ e^t \sin t \\ e^t \end{pmatrix},$$

$$\mathbf{r}_4(t) = \begin{pmatrix} t \sin t + \cos t \\ t \cos t - \sin t \\ t^2 \end{pmatrix} \quad (t > 0).$$

3. Consider the parametric curve given by:

$$\mathbf{x}(t) = \begin{pmatrix} e^t \cos t \\ e^t \sin t \\ e^t \end{pmatrix}$$

- Find the unit tangent, normal, and binormal vectors.
- Find the arc length from $t = 0$ to $t = \pi$.
- Parametrize the line that is tangent to $\mathbf{x}(t)$ at the point t_0 .
- Find the point where the above tangent line intersects the xy -plane. Let $\mathbf{y}(t_0)$ be the position vector for this point. As t_0 varies, sketch the curve that $\mathbf{y}(t_0)$ traces.



4.

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