

1. For each of the following, find the equations for the tangent plane at the given point P on the given surface. Decide whether z can be written as a function of x and y at the point P .

(a) $x^2 + y^2 - z^2 = 18$, $P(3, 5, -4)$

(b) $x^2 - xy - y^2 - z = 0$, $P(1, 1, -1)$

(c) $x^3y^3 + z^3 = 0$, $P(0, 0, 1)$

(d) $z = 4x^2 + y^2$, $P(1, 1, 5)$

2. Suppose that at the point $(1, 2)$, the function $f(x, y)$ has a derivative of $9\sqrt{5}$ in the direction toward $(4, 6)$ and a derivative of $7\sqrt{5}$ in the direction toward $(6, 14)$. Find the derivative of f at $(1, 2)$ in the direction toward the point $(0, 6)$.
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3. (a) Suppose that a nonzero vector in the plane has coordinates (a, b) . How many vectors are perpendicular to it? How many of these are of the same magnitude as (a, b) ? Can you find the coordinates of those?
- (b) Suppose that a nonzero vector in space has coordinates (a, b, c) . Can you describe the vectors that are perpendicular to it? Can you cook them up easily?
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4. For a differentiable function $f(x, y, z)$, how do you compute $D_{\mathbf{i}}f$, $D_{\mathbf{j}}f$, and $D_{\mathbf{k}}f$?
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5. What is the largest value that the directional derivative of $f(x, y, z) = xyz$ can have at the point $(1, 1, 1)$?
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6. Let $f(x, y) = x \cos(y) + e^x y$ and let P be the point $(2, 0)$.

(a) Find the gradient ∇f at P .

(b) For the vector $\mathbf{v} = (-3, 4)$, find the directional derivative of f at P in the direction of \mathbf{v} .

(c) Find a vector that is tangent to the level curve $f(x, y) = 3$ at P .

(d) Find a direction in which f neither increases nor decreases at P .

(e) What is the maximal directional derivative at P ? What is a direction corresponding to this?
