

1. Compute the following integrals. If asked, also change the order of integration. You may use whichever coordinate system you choose.

(a)  $\int_{-3}^2 \int_0^{y^2} (x^2 + y) dx dy$

(b)  $\int_0^1 \int_x^1 xy dy dx$ . Change the order of integration.

(c)  $\int_D \cos(x^2 + y^2) dA$ , where  $D$  is the region  $x^2 + y^2 \leq 1$ .

(d)  $\int_C f(x, y, z) dV$  where  $C$  is the region inside the cylinder  $x^2 + y^2 \leq 9$  and where  $-1 \leq z \leq 2$ , and  $f(x, y, z) = z\sqrt{x^2 + y^2}$ .

(e)  $\int_C f(x, y, z) dV$ , where  $C$  is the unit sphere  $x^2 + y^2 + z^2 \leq 1$  and  $f(x, y, z) = \frac{1}{x^2 + y^2 + z^2}$ .

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2. For the following change of variables, compute  $dA$ .

(a)  $f(u, v) = \left(\frac{u}{2} - \frac{3v}{4}, \frac{v}{4}\right)$

(b)  $x = 2u + 3v$  and  $y = 2u - 3v$ .

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3. Find the average value of the function  $f(x, y) = 3e^y\sqrt{x + e^y}$  over the rectangle  $R = [0, 1] \times [0, 3]$ .
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4. A rod has length 2 meters. At a distance  $x$  meters from the left endpoint of the rod, the density is given by  $\delta(x) = 2 + 6x$  gm/m. Find the total mass of the rod.
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5. The density of electric charge is  $\rho(x, y) = xy$  distributed over a region  $D = \{(x, y) | 1 - x \leq y \leq 1, 0 \leq x \leq 1\}$ . Find the total charge.
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6. Find the mass of the triangle with vertices  $A(0, 0)$ ,  $B(1, 0)$  and  $C(0, 2)$  and density  $\rho(x, y) = 1 + 3x + y$ .
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7. Convert

$$\int_0^3 \int_0^{\sqrt{9-y^2}} \int_{\sqrt{x^2+y^2}}^{\sqrt{18-x^2-y^2}} (x^2 + y^2 + z^2) dz dx dy$$

into spherical coordinates.

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