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1. Find the work done by the vector field  $\mathbf{F} = y\mathbf{i} - x\mathbf{j}$  along the boundary of the hemisphere  $x^2 + y^2 + z^2 = 9$ ,  $z \geq 0$ , oriented counterclockwise, in two ways: First, compute the line integral directly, then, use Stoke's theorem.
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2. Find the circulation of the field  $\mathbf{F} = \begin{pmatrix} x^2 - y \\ 4z \\ x^2 \end{pmatrix}$  around the curve  $C$  in which the plane  $z = 2$  meets the cone  $z = \sqrt{x^2 + y^2}$ , counterclockwise as viewed from above.
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3. Evaluate  $\oint_C \mathbf{F} \cdot d\mathbf{s}$  if  $\mathbf{F} = \begin{pmatrix} xz \\ xy \\ 3xz \end{pmatrix}$  and  $C$  is the boundary of the portion of the plane  $2x + y + z = 2$  in the first octant, traversed counterclockwise when viewed from above.
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4. Calculate the work done by the vector field  $\mathbf{F} = (y^2 + z^2)\mathbf{i} + (x^2 + y^2)\mathbf{j} + (x^2 + y^2)\mathbf{k}$  over the curve  $C$  which is the boundary of the square formed by the lines  $x = \pm 1$ ,  $y = \pm 1$ , traversed counterclockwise when viewed from above.
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5. Let  $\mathbf{F} = \begin{pmatrix} y \\ x^2 \\ (x^2 + y^2)^{3/2} \sin e^{\sqrt{xyz}} \end{pmatrix}$ . Find the outward flux of  $\nabla \times \mathbf{F}$  over the elliptical surface  $\Sigma$  defined by  $4x^2 + 9y^2 + 36z^2 = 36$ ,  $z \geq 0$ .
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6. Let  $f(x, y, z) = (x^2 + y^2 + z^2)^{-1/2}$ . Show that the clockwise circulation of the field  $\mathbf{F} = \nabla f$  around the circle  $x^2 + y^2 = a^2$  in the  $xy$ -plane is zero by applying Stokes' Theorem.
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7. Find the outward flux of  $\mathbf{F} = x^2\mathbf{j} - xz\mathbf{k}$  through the surface cut out from the parabolic cylinder  $y = x^2$ ,  $-1 \leq x \leq 1$ , by the planes  $z = 0$  and  $z = 2$ .
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8. Find the outward flux of  $\mathbf{F} = xy\mathbf{i} - z\mathbf{k}$  through the closed cone  $z = \sqrt{x^2 + y^2}$ ,  $0 \leq z \leq 1$ , that is, the union of the cone and a disk in the plane  $z = 1$ . Then find the flux through the open cone (that is, the one without the disk on top).